

Max Planck Institute for Demographic Research

An agent-based decision model of migration, embedded in the life course

Anna Klabunde¹ Sabine Zinn² Matthias Leuchter¹

¹Max Planck Institute for Demographic Research

²Leibniz Institute for Educational Trajectories

Table of Contents

Motivation

Statistical model

Data

Multistate modelling

Data challenges

First results

Continuous-time Microsimulation

Decision model

Continuous-time Agent-based model

Demographic events

Network formation

Households

Income and consumption

Migration decision

Conclusion





The problem

7 March 2013 Last updated at 11:17 GMT



Prof says his '13,000 EU migrants' report 'misinterpreted'

By Ed Lowther
Political reporter, BBC News

Romanian Immigration Is Up - But Ukip's Prediction Was Off By A Pretty Long Way

The Huffington Post UK | By Jessica Elgot

Posted: 13/08/2014 16:34 BST | Updated: 13/08/2014 16:59 BST

Published online 26 July 2010 | Nature | doi:10.1038/news.2010.375

News

Mexican 'climate migrants' predicted to flood US

A tenth of Mexico's population could surge north to escape climate-triggered crop failures, study claims.

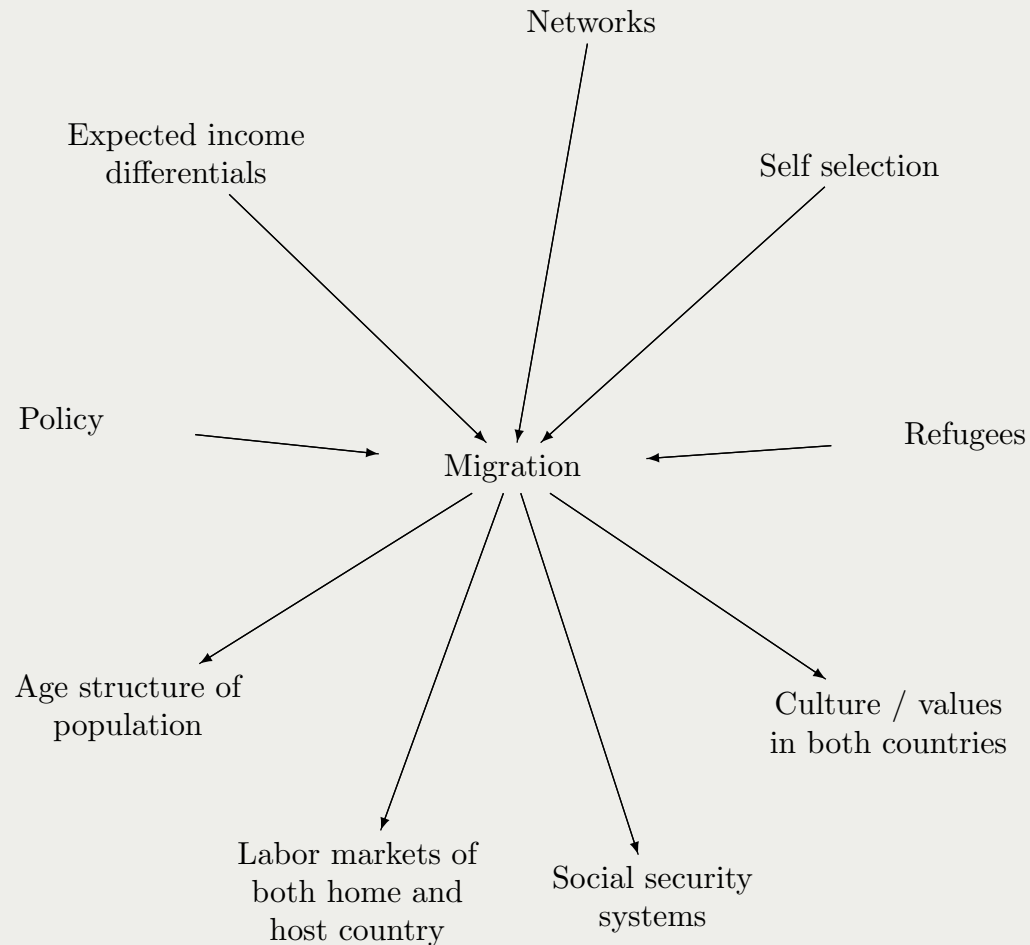
Zoë Corbyn

Gallup World Poll: 14 percent of adults worldwide desire to emigrate (2005).

About 3 percent of people emigrate at some point in their life (IOM 2010).



The phenomenon of international migration



Tools to understand and predict migration I

Statistical models

- ▶ Time series methods (Gorbey et al. 1999)
- ▶ Macro-level econometric models (Dustmann et al. 2003)
- ▶ Bayesian forecasting (Bijak 2011)
- ▶ Extrapolation from stock data (Abel and Sander 2014)
- ▶ Micro-level
 - ▶ Discrete time event-history analysis (Massey and Espinosa 1997)
 - ▶ Survival analysis (Lindstrom 1996)

Microsimulation

Discrete time (Massey and Zenteno 1999) vs. continuous time (Rephann and Holm 2004)



Tools to understand and predict migration II

Theoretical models

- ▶ Mainly econ: Sjaastad (1962), Harris and Todaro (1970), Borjas (1987), Stark and Bloom (1985)...
- ▶ Gravity theory (Stewart 1941)
- ▶ Push-pull theory (Lee 1966)
- ▶ Networks and social capital

Qualitative research

Field studies, In-depth surveys,...

Agent-based models

Klabunde (2014), Kniveton et al. (2011)...



Our approach

Idea: Combine ‘statistical individual’ (Courgeau 2012) and ‘agent’

Statistical model

Multistate survival analysis on the MAFE data set

Microsimulation

Synthetic life courses prescribed by estimated event rates

Theoretical model for migration behavior

Process Theory of Planned Behavior (Ajzen 1991 / Willekens 2014)

Agent-based model

Putting it all together, adding spatial dimension and interaction



The MAFE Senegal data set I

- ▶ <http://mafeproject.site.ined.fr/>
- ▶ Coordinated by INED; Cooperation of 9 institutions
- ▶ Event-history microsurvey, similar to the Mexican Migration Project
- ▶ Focus: Migration flows between Senegal and France, Italy, Spain
- ▶ Household survey: 1141 households in Senegal; basic information on 12350 individuals
- ▶ Biograph survey: 1062 in Senegal, ca. 200 in each of France, Italy, Spain
- ▶ Oversampling of migrant households (household survey), return migrants and partners of migrants (Biograph survey)



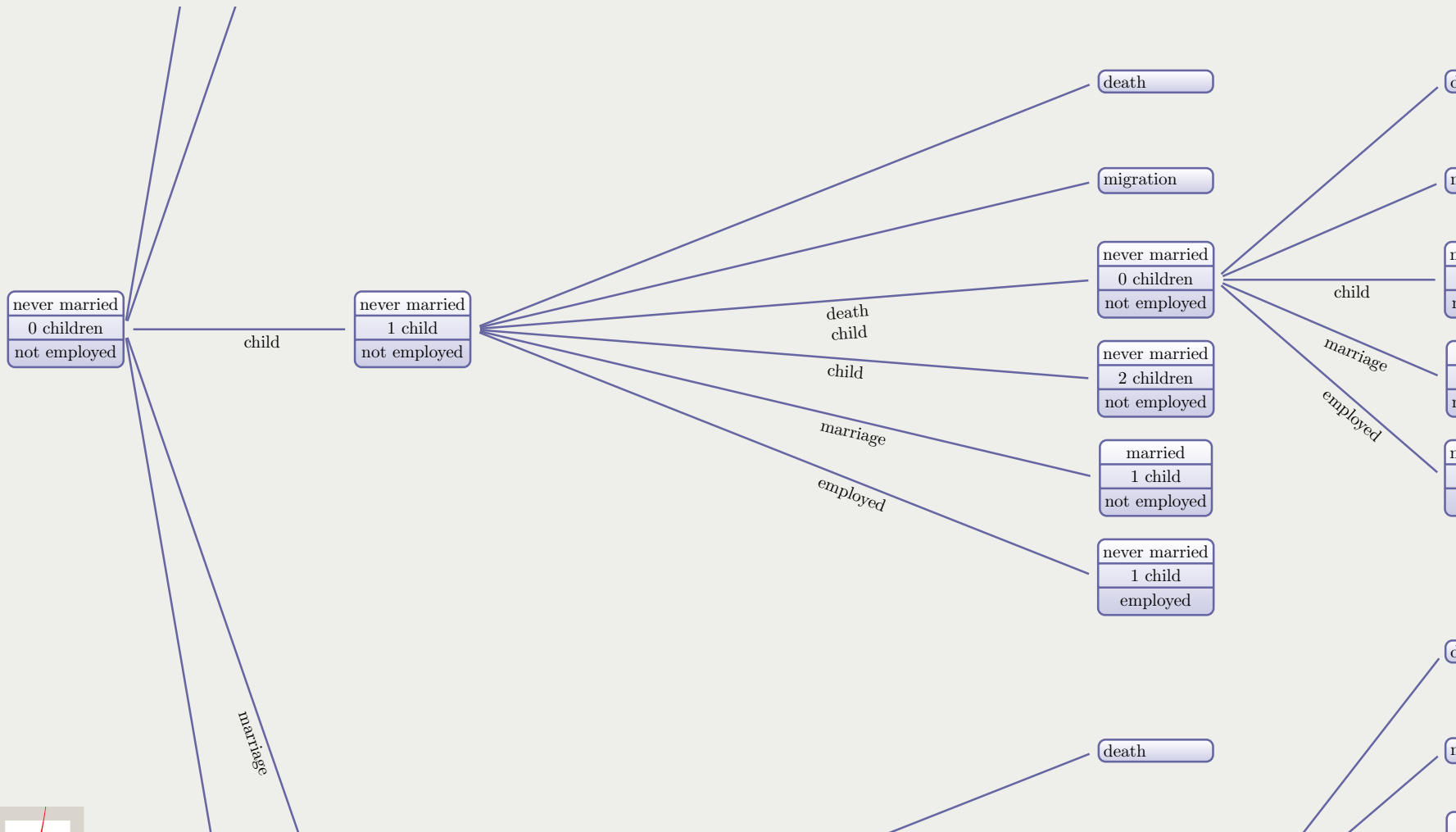
The MAFE Senegal data set II

- ▶ Senegal: 3-stage stratified random sample from Dakar region
 - ▶ 10 strata of equal size (according to the % of households with migrants within each of them)
 - ▶ 60 districts were selected (6 per strata)
 - ▶ 22 households were randomly selected in each of the 60 districts
 - ▶ Two strata: the households with migrants and those without
 - ▶ Households equally divided: 11 households with migrants and 11 without
 - ▶ Total of 1320 households (449 with migrants and 841 without)
 - ▶ Completed household surveys: 1141.
- ▶ In Italy and France: selected public places and snowballing
- ▶ Spain: Sampling from the Municipal Population Register





Multistate model I





Multistate model II

- ▶ Life histories are realisations of a continuous-time Markov process
- ▶ Times at which events occur are random
- ▶ Waiting times to events stem from an exponential distribution
- ▶ Rate of transition out of the current state is the parameter of this distribution





Multistate model III

- ▶ Different new states are competing risks with a transition rate specific to the new states
- ▶ Transition rates vary with age (and possibly other covariates)
- ▶ Occurrence-exposure rates; piecewise-constant in age-interval
- ▶ implemented with the R package 'Biograph' (Willekens 2013)





Transitions observed - women

	S	Ch	M	E	D	W	Total	Censored	TOTAL
S	0	99	635	74	0	0	808	60	868
Ch	0	1591	83	113	122	87	1996	371	2367
M	0	636	0	67	44	15	762	65	827
E	0	0	0	0	0	0	0	273	273
D	0	32	77	11	0	0	120	46	166
W	0	8	32	8	0	0	48	54	102
Total	0	2366	827	273	166	102	3734	869	4603





Transitions observed - men

	S	M	E	D	W	Total	Censored	TOTAL
S	0	458	193	0	0	651	147	798
M	0	126	135	105	21	387	271	658
E	0	0	0	0	0	0	333	333
D	0	66	4	9	1	80	34	114
W	0	8	1	0	0	9	13	22
Total	0	658	333	114	22	1127	798	1925





Challenges: Polygamy

- ▶ Of 590 women married at survey date (2008)
 - ▶ 390 were the only wife
 - ▶ 129 had one co-wife, 61 had 2 co-wives, 9 had 3 co-wives and one had 13 co-wives
 - ▶ i.e. 33.9 % of married women live in polygamous marriages
- ▶ For men at survey date:
 - ▶ 17.3% of married men have more than one wife



Challenges: Non-representativity, weighting

- ▶ Only observations in Dakar region
 - ▶ 26% of population, but only 0.28% of land surface
 - ▶ internal migration to Dakar
 - ▶ in Dakar 26% below Senegalese poverty threshold; rest of country: between 40 and 77 % (ANSD Senegal, 2011)
 - ▶ More than 50% of public spending for Dakar (World Bank 2012)
- ▶ Migrants oversampled
 - ▶ Weights for estimation of rates and descriptive statistics
 - ▶ weighting factor: inverse of sampling probabilities at each stage, normalized and corrected for non-response





Challenges: Income, Truncation

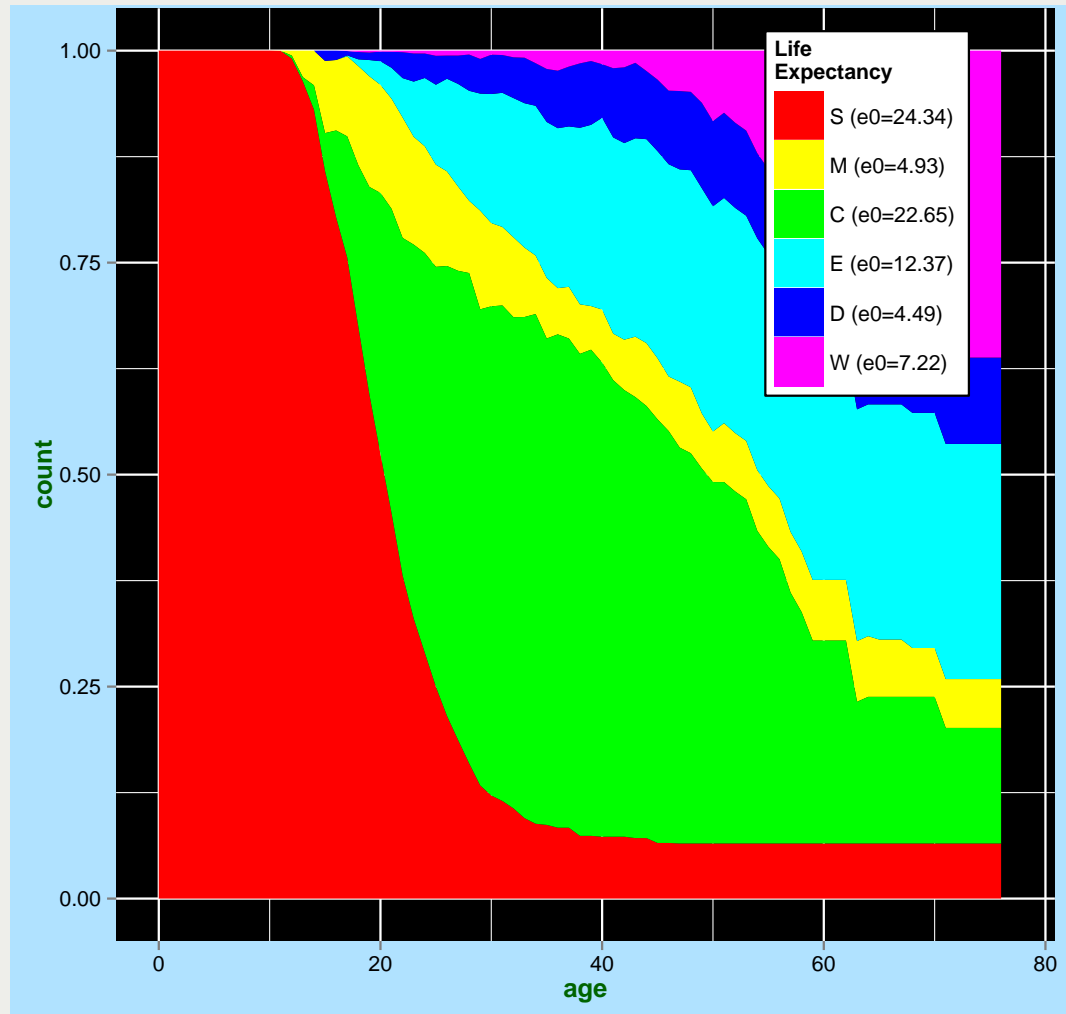
- ▶ More than 50% missing observations for sources of income
- ▶ Any virtual cohorts or period-populations constructed from the retrospective data are conditioned upon survival to the year 2008
- ▶ → Other sources for mortality rates





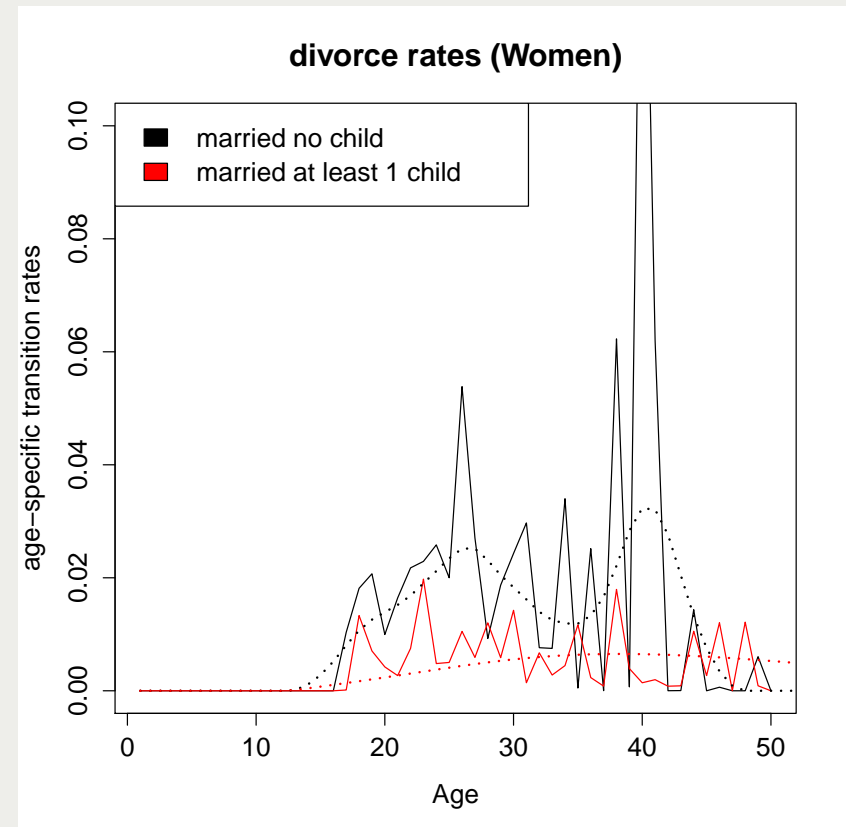
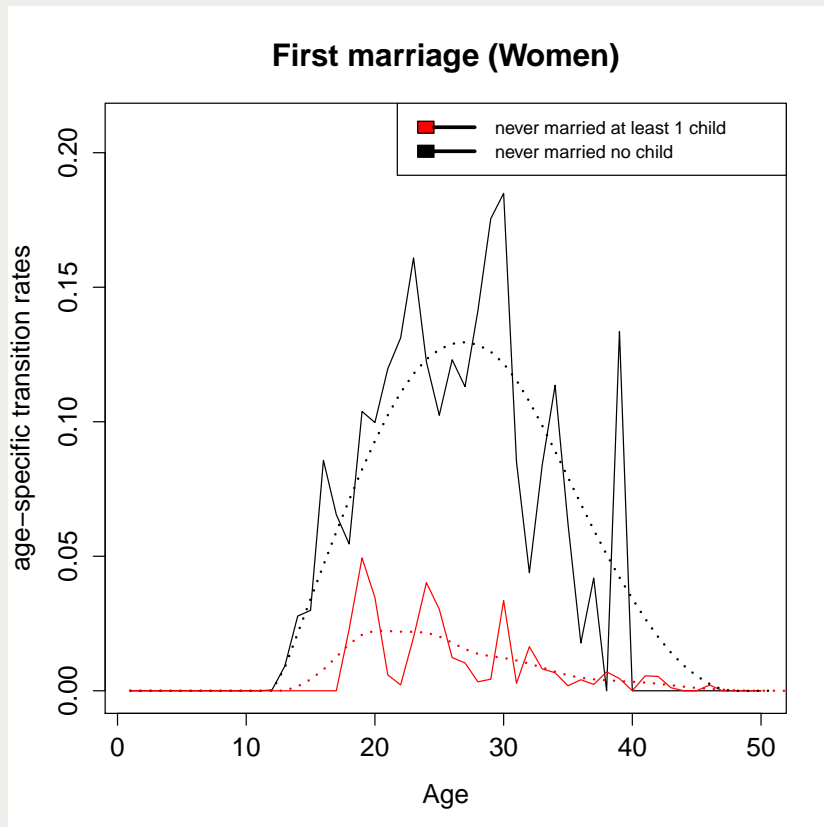
First results

Expected duration in different states



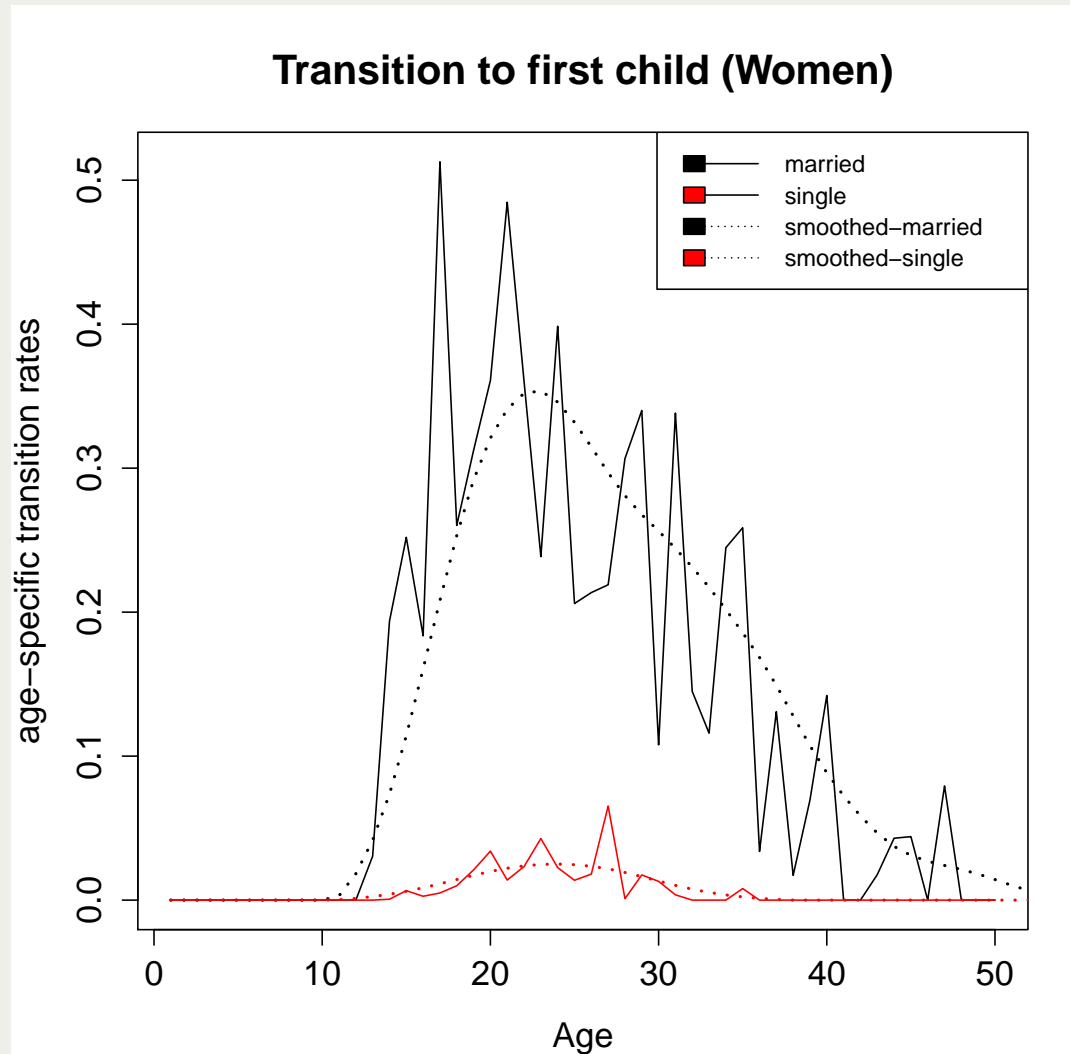


Marriage and divorce





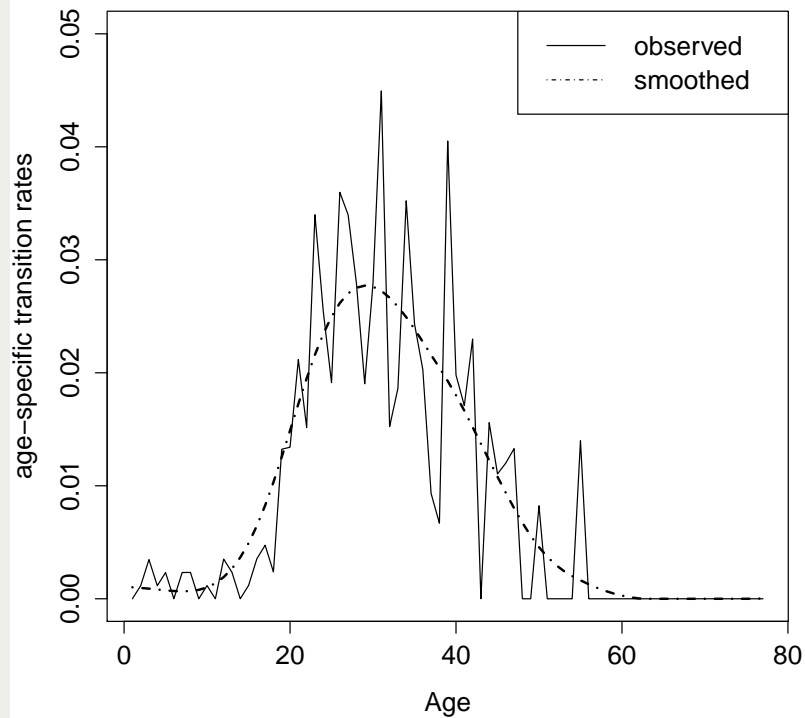
Fertility



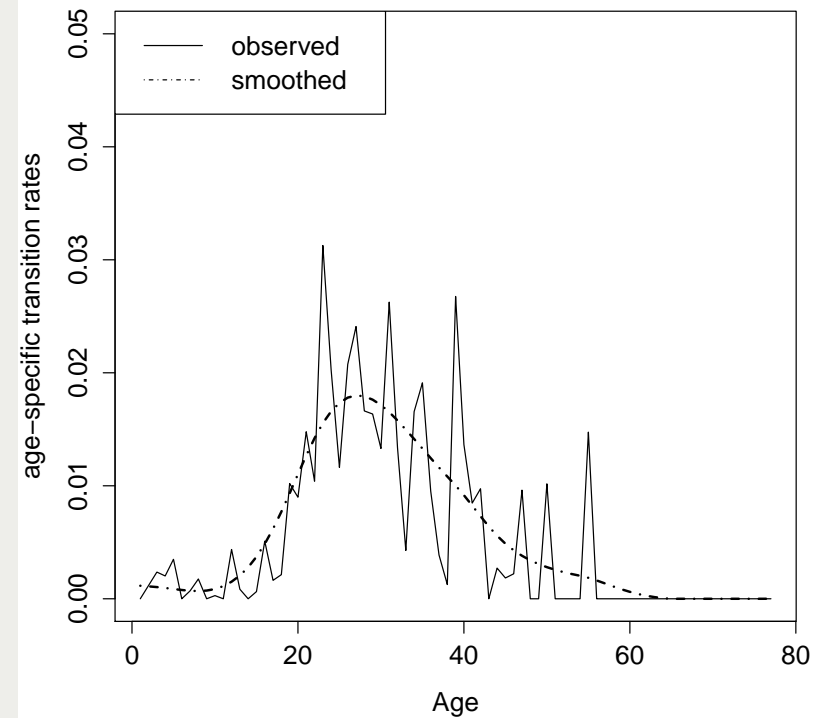


Emigration rates

emigration rates (Women-unweighted)



emigration rates (Women-weighted)



State space

Nr.	State	Possible new states
1	(NM, 0, NE)	(M, 0, NE), (NM, 1, NE), (NM, 0, E), Mig, De
2	(M, 0, NE)	(W, 0, NE), (D, 0, NE), (M, 1, NE), (M, 0, E), Mig, De
3	(NM, 1, NE)	(M, 1, NE), (NM, 0, NE), (NM, 2, NE), (NM, 1, E), Mig, De
4	(NM, 0, E)	(M, 0, E), (NM, 1, E), (NM, 0, NE), Mig, De
5	(W, 0, NE)	(M, 0, NE), (W, 1, NE), (W, 0, E), Mig, De
6	(D, 0, NE)	(M, 0, NE), (D, 1, NE), (D, 0, E), Mig, De
7	(M, 1, NE)	(W, 1, NE), (D, 1, NE), (M, 0, NE), (M, 2, NE), (M, 1, E), Mig, De
8	(M, 0, E)	(W, 0, E), (D, 0, E), (M, 1, E), (M, 0, NE), Mig, De
9	(NM, 2, NE)	(M, 2, NE), (NM, 1, NE), (NM, 3, NE), (NM, 2, E), Mig, De
10	(NM, 1, E)	(M, 1, E), (NM, 0, E), (NM, 2, E), (NM, 1, NE), Mig, De
11	(W, 1, NE)	(M, 1, NE), (W, 0, NE), (W, 2, NE), (W, 1, E), Mig, De
12	(W, 0, E)	(M, 0, E), (W, 1, E), (W, 0, NE), Mig, De
13	(D, 1, NE)	(M, 1, NE), (D, 0, NE), (D, 2, NE), (D, 1, E), Mig, De
14	(D, 0, E)	(M, 0, E), (D, 1, E), (D, 0, NE), Mig, De
15	(M, 2, NE)	(W, 2, NE), (M, 1, NE), (D, 2, NE), (M, 3, NE), (M, 2, E)
16	(M, 1, E)	(W, 1, E), (D, 1, E), (M, 0, E), (M, 2, E), (M, 1, NE), Mig, De
17	(NM, 3, NE)	(M, 3, NE), (M, 2, NE), (NM, 3+, NE), (NM, 3, E), Mig, De
18	(NM, 2, E)	(M, 2, E), (NM, 1, E), (NM, 3, E), (NM, 2, NE), Mig, De
19	(W, 2, NE)	(M, 2, NE), (W, 1, NE), (W, 3, NE), (W, 2, E), Mig, De
20	(W, 1, E)	(M, 1, E), (W, 0, E), (W, 2, E), (W, 1, NE), Mig, De
21	(D, 2, NE)	(M, 2, NE), (D, 1, NE), (D, 3, NE), (D, 2, E), Mig, De
22	(D, 1, E)	(M, 1, E), (D, 0, E), (D, 2, E), (D, 1, NE), Mig, De
23	(M, 3, NE)	(W, 3, NE), (D, 3, NE), (M, 2, NE), (M, 3+, NE), (M, 3, E), Mig, De
24	(M, 2, E)	(W, 2, E), (D, 2, E), (M, 1, E), (M, 3, E), (M, 2, NE), Mig, De
25	(NM, 3, E)	(M, 3, E), (NM, 2, E), (NM, 3+, E), (NM, 3, NE), Mig, De
26	(W, 3, NE)	(M, 3, NE), (W, 2, NE), (W, 3+, NE), (W, 3, E), Mig, De
27	(W, 2, E)	(M, 2, E), (W, 1, E), (W, 3, E), (W, 2, NE), Mig, De
28	(D, 3, NE)	(M, 3, NE), (D, 2, NE), (D, 3+, NE), (D, 3, E), Mig, De
29	(D, 2, E)	(M, 2, E), (D, 1, E), (D, 3, E), (D, 2, NE), Mig, De
30	(W, 3, NE)	(M, 3, NE), (W, 2, NE), (W, 3+, NE), (W, 3, E), Mig, De
31	(D, 3, NE)	(M, 3, NE), (D, 2, NE), (D, 3+, NE), (D, 3, E), Mig, De
32	(M, 3, E)	(W, 3, E), (D, 3, E), (M, 2, E), (M, 3+, E), (M, 3, NE), Mig, De
33	(W, 3, E)	(M, 3, E), (W, 2, E), (W, 3+, E), (W, 3, NE), Mig, De
34	(D, 3, E)	(M, 3, E), (D, 2, E), (D, 3+, E), (D, 3, NE), Mig, De



Synthetic life courses

- ▶ *Micsim* Package (Zinn 2014)
- ▶ Synthetic initial population derived from survey population
- ▶ Synthetic life courses: described by a non-homogeneous continuous-time Markov process
- ▶ Transition rates from MAFE
- ▶ Waiting times drawn from corresponding distributions, one for each possible new state
- ▶ Event with the shortest waiting time occurs (competing risks)
- ▶ All transitions simulated except migration (decision model)



Migration decision model: Theory of planned behavior

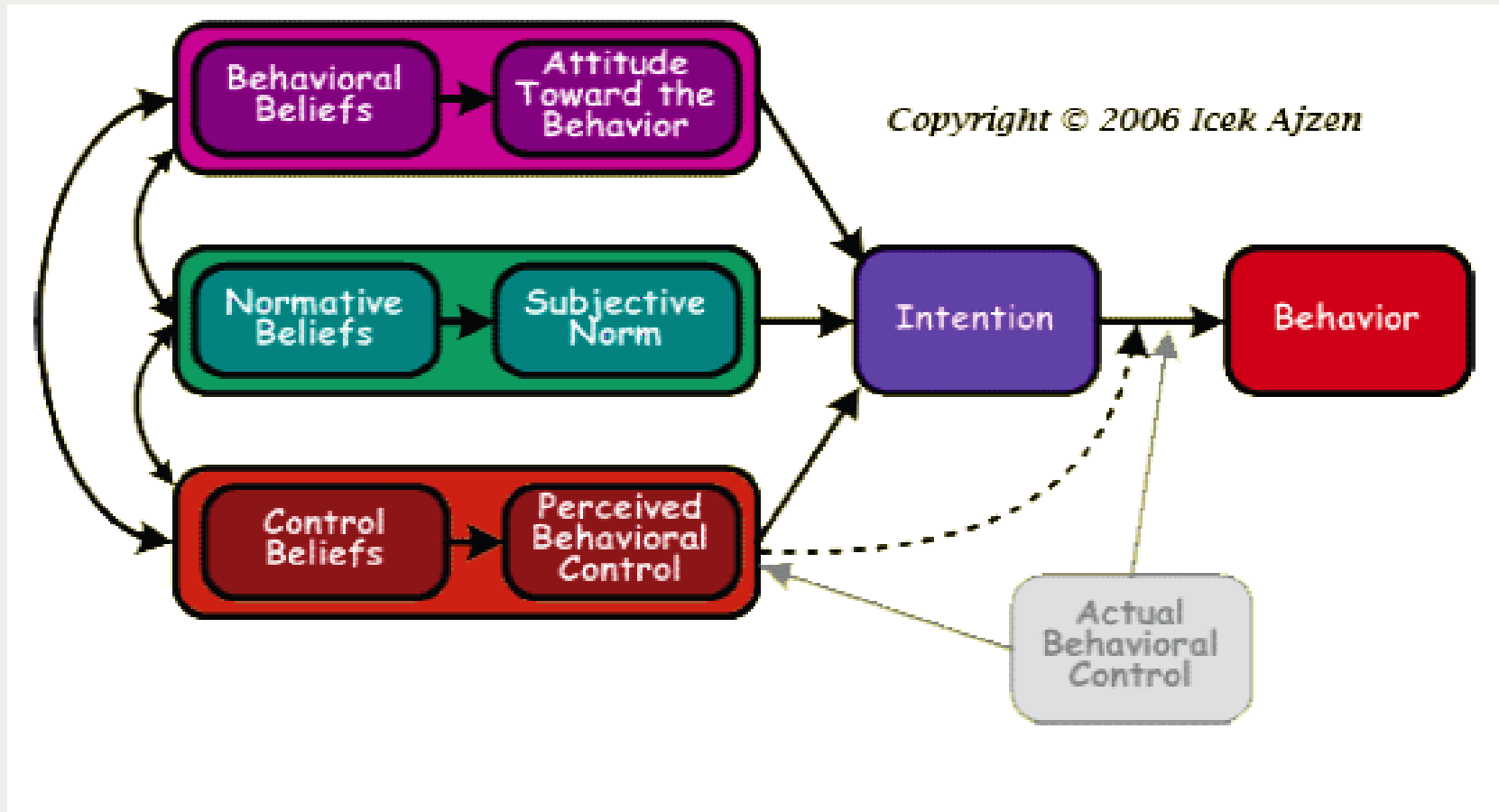


Figure: Fishbein and Ajzen (2010)



TPB applied to migration I

- ▶ See also: De Jong (2000), Van Dalen and Henkens (2008), Gubhaju and De Jong (2009)
- ▶ In our model: Agents pursue happiness, influenced by income and being close to family
- ▶ Attitude:

$$A_{i,t} = ew_{i,t}bw_{i,t} + ef_{i,t}bf_{i,t} \quad (1)$$

where ew : evaluation of higher income in the host country, bw : subjective probability to achieve higher income, ef : evaluation of family reunification, bf : subjective probability to achieve family reunification.



TPB applied to migration II

- ▶ Evaluation of higher income in the host country:

$$ew_{i,t} = a_1 c_{h,t} + a_2 w_{i,t} + a_3 (A_{h,t} + K_{h,t}) \quad (2)$$

where $c_{h,t}$: capital of i 's household, $w_{i,t}$: agent's wage earnings, $A_{h,t}$: number of adults in the household, $K_{h,t}$: number of children, a_1 , a_2 and a_3 : parameters

- ▶ Subjective probability to achieve higher income through migration: proportion of agent's network neighbors who had higher income after migration than the agent's current income
- ▶ Evaluation of family reunification: $ef_{i,t} = a_4 M_{i,t}$, where $M_{i,t}$ is the number of previous household members who have migrated and a_4 is a fixed parameter
- ▶ Subjective probability of family reunification: 1



TPB applied to migration III

- ▶ Social norms: prop. of network neighbors who ever migrated
- ▶ Perceived behavioural control:

$$PBC_{i,t} = -(pb_t cb_{i,t} + pc_{i,t} cc_{i,t}) \quad (3)$$

where pb_t : importance of border enforcement, $cb_{i,t}$: subjective probability that border enforcement will influence the agent's migration, $pc_{i,t}$: importance of the migration cost, $cc_{i,t}$: subjective probability that the migration cost could preclude the agent's migration.

- ▶ Border enforcement pb_t : exogenously given and known; $cb_{i,t}$: proportion of failed migration attempts of the agent's network neighbors; $pc_{i,t}$ exogenous and constant
- ▶ $cc_{i,t}$: proportion of periods in which the agent would not have been able to afford the migration cost





TPB applied to migration IV

- ▶ Intention:

$$I_{i,t} = a_5 A_{i,t} + a_6 SN_{i,t} + a_7 PBC_{i,t} \quad (4)$$

where a_5 , a_6 and a_7 are parameters.

- ▶ Attitude and social norms: positive values, PBC is negative
- ▶ Agent's intention $I_{i,t}$ can be in the range $[-\text{inf}, +\text{inf}]$.

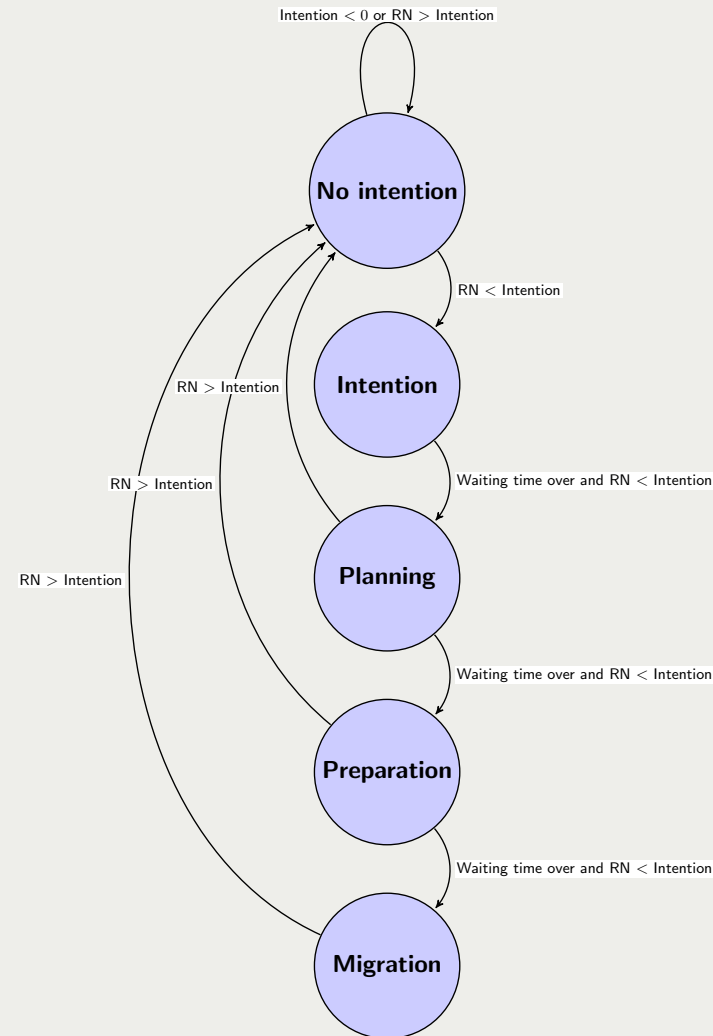


Why the TPB is reasonable for the migration decision

- ▶ Established theory from social psychology
- ▶ Empirically relevant predictor of behavior (see Armitage and Conner 2001)
- ▶ Far-reaching consequences
- ▶ High level of uncertainty
- ▶ Enables rigorous inclusion of factors influencing beliefs
- ▶ Attrition during the decision process and time dimension (Willekens 2014)



Transforming the TPB into a process theory





Continuous-time Agent-based model: Overview I

- ▶ Microsimulation determines demographic events and waiting times for each agent
- ▶ Autonomous agents make migration decision following TPB
- ▶ Also ABM is continuous time (milliseconds)
- ▶ Only eventful milliseconds are simulated
- ▶ Agents act when waiting times are over or triggered by actions of other agents
- ▶ Demographic events and transitions to new decision stages are competing risks





Continuous-time Agent-based model: Overview II

- ▶ The following events happen in the order they are scheduled:
 - ▶ Births, deaths
 - ▶ Marriage, divorce
 - ▶ Transitions to employment and unemployment
 - ▶ Retirement
 - ▶ Update of intention to migrate
 - ▶ Drop out of decision stages and progress to next stage
 - ▶ Migration
- ▶ At the end of each day: Consumption
- ▶ At the end of each month: Employed agents receive wage





Continuous-time Agent-based model: Overview III

- ▶ Agents live in households
- ▶ Income sharing in households
- ▶ Fixed network from birth
- ▶ Two stylized countries
- ▶ Two-dimensional grid
- ▶ No choice of exact location in this version





Demographic events

- ▶ From MAFE, via Micsim
- ▶ Agents 'receive' a mostly pre-determined life history; deterministic
- ▶ In this version: Marriage, fertility etc have impact on migration but not vice versa → Questionable!
- ▶ Only covariates for rates: age and gender (later: educational level, parity)
- ▶ Due to marriage and household formation: Some demographic events happen deterministically





Network formation

- ▶ At birth, links are formed to
 - ▶ Parents, siblings
 - ▶ Other household members
 - ▶ All members of all households in the Moore neighborhood
- ▶ Links remain throughout life



Marriage market I

- ▶ Modelled after Zinn (2012)
- ▶ 6 months before marriage event is scheduled: agent joins marriage market
- ▶ Compatibility score: Logit estimation on MAFE data which predicts the probability to be married to an individual with given characteristics
- ▶ Every 2nd time an individual enters the marriage market: mating
- ▶ If there are agents whose scheduled marriage time has already passed, the agent with the earliest marriage time is chosen
- ▶ Otherwise, the person with the marriage time closest to the current date





Marriage market II

- ▶ This agent makes partner choice: Choose partner in marriage market with highest compatibility score
- ▶ Newly married agents form household





Divorce and widowhood

- ▶ Women experience divorce event
- ▶ Household dissolution
- ▶ Ex-husband is assigned new waiting time to re-marriage based on MAFE transition rate for divorced men of his age (may be infinite)
- ▶ Re-marriage
- ▶ Widowhood if partner dies
- ▶ Analogous: new waiting time to re-marriage





Income and consumption

- ▶ Employed agents receive wage at the end of the month
- ▶ All earnings are added to household capital
- ▶ Different wage distributions in the two countries
- ▶ In the host country: wage is increased by dw if the agent has network neighbors there
- ▶ Every day, household capital $c_{h,t}$ is updated after consumption:

$$c_{h,t} = c_{h,t-1} - A_{h,t} \frac{m_1}{30} - K_{h,t} \frac{m_2}{30} \quad (5)$$

where $A_{h,t}$: number of adults in the household; $K_{h,t}$: number of children; m_1 : Adult monthly consumption; m_2 : Child monthly consumption



Migration decision

- ▶ Intention:

$$I_{i,t} = a_5 A_{i,t} + a_6 SN_{i,t} + a_7 PBC_{i,t} \quad (6)$$

- ▶ If intention is negative: agent drops out of decision process
- ▶ If intention is positive: value is transformed to a probability to move to the next decision stage:

$$prob_{i,t} = \frac{1}{1 + \exp(-I_{i,t})} \quad (7)$$

- ▶ Agent makes a random draw from the interval $[0, 1]$
- ▶ If the value drawn is smaller than $prob_{i,t}$, the agent moves to the next decision stage
- ▶ Otherwise, the agent exits his current stage and moves back to the beginning of the decision making process





Moving between decision stages I

- ▶ Once an agent enters a new stage: rate of moving to the next stage is determined using an exponential survival model with the intention as the only idiosyncratic parameter
- ▶ Probability density function of the exponential distribution:

$$p(t; \lambda_{i,t}) = \lambda_{i,t} e^{-t\lambda_{i,t}} \quad (8)$$

- ▶ Expected waiting time: $1/\lambda_{i,t}$
- ▶ The idiosyncratic parameter $\lambda_{i,t}$ is:

$$\lambda_{i,t}(\rho, l_{i,t}) = \rho e^{a_8 * l_{i,t}} \quad (9)$$

where ρ : baseline rate for an intention value of 0; $l_{i,t}$: intention computed in 6; a_8 : parameter.





Moving between decision stages II

- ▶ Same for agents currently in the “no intention” stage
- ▶ Entering new decision stage in the migration decision process and experiencing a new demographic event are competing risks
- ▶ If a demographic event happens to an individual before the waiting time to the next decision stage is over:
- ▶ New intention value is computed right away after the demographic event to compute new waiting time for the next step
- ▶ Reason: demographic event can change the evaluation of the attractiveness and feasibility of migration dramatically





Migration I

- ▶ Intention one more time, random draw
- ▶ If this random number is smaller than $prob_{i,t}$, the agent finally attempts migration
- ▶ Actual border control pb_t
- ▶ Agent's probability to successfully migrate $probm_{i,t}$ is determined as

$$probm_{i,t} = \frac{1}{1 + \exp\left(-\frac{1}{pb_t}\right)}, pb_t > 0 \quad (10)$$

- ▶ Random draw
- ▶ If successful: Agent changes location, becomes unemployed





Migration II

- ▶ If the agent is unmarried or the spouse is still in the home country: migrant still belongs to his former home country household (remittances)
- ▶ If the agent is married and the spouse migrated before him: Both spouses form new household in the host country
- ▶ If the migration attempt is unsuccessful the agent remains in the home country and moves back to the first decision stage.





Next steps

- ▶ Finish programming
- ▶ Finish estimating rates
- ▶ Allow for polygamous marriages?
- ▶ Iterative calibration procedure
- ▶ Ranges of parameters from MAFE; systematic sensitivity analysis
- ▶ Verify whether model produces empirical migration rates
- ▶ Most important model extension: Education
- ▶ What-if research questions can be answered



Conclusion

- ▶ TPB might help avoid wrong predictions
 - ▶ Attitude alone overpredicts migration
 - ▶ Change in policy has effect on PBC without affecting attitude. Not taking this into consideration underpredicts migration
 - ▶ Changes in attitudes and social norms take time; effects might be delayed
 - ▶ What counts is not actual probabilities, but subjective beliefs (Bounded rationality!)
- ▶ Hope: Combine state-of the art statistical analysis of life courses with module to handle interaction and non-linear decision-making → better policy analysis and predictions





References I

- 📄 Abel, G. J., & Sander, N. (2014). Quantifying global international migration flows. *Science* 343: 1520–1522.
- 📄 Ajzen, I. (1991). The theory of planned behaviour. *Organizational Behaviour and Human Decision Processes* 50:179–211
- 📄 Armitage, C. J., & Conner, M. (2001). Efficacy of the theory of planned behaviour: A meta-analytic review. *British journal of social psychology* 40:471–499.
- 📄 Bijak, J. (2011): *Forecasting International Migration in Europe*. Springer, Dordrecht.
- 📄 Borjas G.J. (1987). Self-Selection and the Earnings of Immigrants. *The American Economic Review* 77:531–553



References II

- 📄 Courageau, D. (2012). Probability and Social Science. Methodological Relationships between the two Approaches. Springer, Dordrecht.
- 📄 Esipova, N., Ray, J. & A. Pugliese (2011) Gallup World Poll: The many faces of migration. International Organization for Migration (IOM), Geneva, in cooperation with GALLUP. IOM Migration Research Series No. 43
- 📄 De Jong, G. F. (2000). Expectations, gender, and norms in migration decision-making. Population studies 54:307–319
- 📄 Dustmann, C., Casanova, M., Fertig, M., Preston, I., Schmidt, C.M., (2003) The impact of EU enlargement on migration flows. (Home Office Online Report 25/03). Research Development and Statistics Directorate, Home Office: London, UK





References III

- 📄 Fishbein, M., & Ajzen, I. (2010). Predicting and changing behaviour: The reasoned action approach. New York: Psychology Press (Taylor & Francis)
- 📄 Gorbey, S., James, D., & Poot, J. (1999). Population forecasting with endogenous migration: an application to Trans-Tasman migration. *International Regional Science Review* 22: 69–101
- 📄 Gubhaju, B., & De Jong, G. F. (2009). Individual versus household migration decision rules: Gender and marital status differences in intentions to migrate in South Africa. *International Migration* 47:31–61.



References IV

- 📄 Harris, J.R. & Todaro, M.P. (1970). Migration, Unemployment and Development: A Two-Sector Analysis. *The American Economic Review* 60:126–142
- 📄 International Organization for Migration (2010) *World Migration Report 2010*. IOM, Geneva
- 📄 Klabunde, A. (2014) *Computational Economic Modeling of Migration*, in: Shu-Heng Chen and Mak Kaboudan (editors): *Oxford University Press Handbook on Computational Economics and Finance*. Oxford University Press (forthcoming)
- 📄 Kniveton, D. R., Smith, C. D.& Wood, S. (2011). Agent-based model simulations of future changes in migration flows for Burkina Faso. *Global Environmental Change*, 21, Supplement 1: S34–S40.



References V

- 📄 Lee, E. S. (1966). A theory of migration. *Demography* 3:47–57.
- 📄 Lindstrom, D. P. (1996). Economic opportunity in Mexico and return migration from the United States. *Demography* 33:357–374.
- 📄 Massey, D. S., & Espinosa, K. E. (1997). What's driving Mexico-US migration? A theoretical, empirical, and policy analysis. *American Journal of Sociology* 102:939–999.
- 📄 Massey, D. S., & Zenteno, R. M. (1999). The dynamics of mass migration. *Proceedings of the National Academy of Sciences* 96:5328–5335



References VI

- 📄 Rephann, T. J., & Holm, E. (2004). Economic-demographic effects of immigration: Results from a dynamic spatial microsimulation model. *International Regional Science Review*, 27:379–410
- 📄 Sjaastad, L.A. (1962). The Costs and Returns of Human Migration. *Journal of Political Economy* 70: 80–93
- 📄 Stark, O. & Bloom, E. (1985) The New Economics of Labor Migration. *The American Economic Review* 75:173–178
- 📄 Stewart, J. Q. (1941). An inverse distance variation for certain social influences. *Science* 93:89–90
- 📄 Tertilt, M. (2005) Polygyny, fertility, and savings. *Journal of Political Economy* 113:1341–1371





References VII

- 📄 Van Dalen, HP and Henkens K. (2008) Emigration Intentions: Mere Words or True Plans? Explaining International Migration Intentions and Behavior. CentER Discussion Paper No. 2008–60, Tilburg University: Tilburg.
- 📄 Willekens, F. (2013) Package *Biograph*. Published on CRAN.
- 📄 Willekens, F. (2014) An agent-based simulation model (ABS) of migration based on the theory of planned behaviour. Paper presented at the workshop ‘Recent Developments and Future Directions in Agent-Based Modelling in Population Studies, Leuven, 18-19 Sept 2014

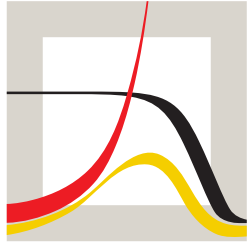




References VIII

- 📄 Zinn, S. (2012): A mate-matching algorithm for continuous-time microsimulation models. *International Journal of Microsimulation* 5:31–51
- 📄 Zinn, S. (2014) Package *MicSim*. Published on CRAN, 2014.





Max Planck Institute for Demographic Research

For more information please see

www.demogr.mpg.de

Contact: Anna Klabunde¹ Sabine Zinn²

Matthias Leuchter¹

¹klabunde@demogr.mpg.de